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APPLICATION NO.	FILING DATE	FIRST NAMED INVENTOR	ATTORNEY DOCKET NO.	CONFIRMATION NO. 🦡
09/669,877	09/27/2000	Randell L. Mills	62-231-1EL	4531
20736 7	590 01/17/2002			
MANELLI DENISON & SELTER			EXAMINER	
2000 M STREET NW SUITE 700 WASHINGTON, DC 20036-3307			LANGEL, WAYNE A	VAYNE A
		•	ART UNIT	PAPER NUMBER
			1754	/ /
			DATE MAILED: 01/17/2002	4

Please find below and/or attached an Office communication concerning this application or proceeding.



	Application No. Applicant(s)				
Office Action Summary	Examiner , Group Art Unit				
	Lange/ 1754				
—The MAILING DATE of this communication appears on the cover sheet beneath the correspondence address—					
Peri d for Response	2				
A SHORTENED STATUTORY PERIOD FOR RESPONSE IS SET TO EXPIRE MONTH(S) FROM THE MAILING DATE OF THIS COMMUNICATION.					
- Extensions of time may be available under the provisions of 37 CFR 1.136(a). In no event, however, may a response be timely filed after SIX (6) MONTHS from the mailing date of this communication. - If the period for response specified above is less than thirty (30) days, a response within the statutory minimum of thirty (30) days will be considered timely. - If NO period for response is specified above, such period shall, by default, expire SIX (6) MONTHS from the mailing date of this communication. - Failure to respond within the set or extended period for response will, by statute, cause the application to become ABANDONED (35 U.S.C. § 133).					
Status					
☐ Responsive to communication(s) filed on	•				
☐ This action is FINAL .					
Since this application is in condition for allowance except for formal matters, prosecution as to the merits is closed in accordance with the practice under Ex parte Quayle, 1935 C.D. 1 1; 453 O.G. 213.					
Disposition of Claims)					
(Claim(s) 1-2-8	is/are pending in the application.				
Of the above claim(s)	is/are withdrawn from consideration.				
	is/are allowed.				
	is/are rejected.				
☐ Claim(s)					
☐ Claim(s)					
	requirement.				
Application Papers					
☐ See the attached Notice of Draftsperson's Patent Drawing Review, PTO-948.					
☐ The proposed drawing correction, filed onis ☐ approved ☐ disapproved. ☐ The drawing(s) filed onis/are objected to by the Examiner.					
☐ The drawing(s) filed on is/are objected to by the Examiner. ☐ The specification is objected to by the Examiner.					
☐ The oath or declaration is objected to by the Examiner.					
Priority under 35 U.S.C. § 119 (a)-(d)					
 □ Acknowledgment is made of a claim for foreign priority under 35 U.S.C. § 11 9(a)-(d). □ All □ Some* □ None of the CERTIFIED copies of the priority documents have been □ received. 					
 □ received in Application No. (Series Code/Serial Number) □ received in this national stage application from the International Bureau (PCT Rule 1 7.2(a)). 					
*Certified copies not received:					
Attachm nt(s)	22.43.				
Attachm nt(s) Information Disclosure Statement(s), PTO-1449, Paper No(s). Interview Summary, PTO-413					
Notice of References Cited, PTO-892	□ Notic of Informal Pat nt Application, PTO-152				
□ Notice of Draftsperson's Patent Drawing R view, PTO-948 □ Other □					
Office Action Summary					

U. S. Patent and Trademark Office PTO-326 (Rev. 3-97) Part of Paper No.

35 U.S.C. § 101 REJECTION

Claims 1-28 are rejected under 35 U.S.C. § 101 because the disclosed invention is inoperative and therefore lacks credible utility. All the claims recite a "neutral, positive or negative increased binding energy species". Page 10, lines 15-23 of the specification discloses that an "increased binding energy one electron atom" has a binding energy given by

Binding Energy = $\frac{2^{2}13.6 \text{ eV}}{(\frac{L}{p})^{2}}$

where p is an integer greater than 1. The claimed compounds would thus constitute compounds having new energy states that are below the conventionally accepted ground state energy. An asserted utility would not be considered credible where a person of ordinary skill would consider the assertion to be incredible in view of contemporary knowledge and where the evidence offered by applicant does not counter what contemporary knowledge otherwise suggests. See MPEP § 2107.01. See the attached Appendix which shows the mathematical justification as to why conventional theory and experiment precludes the existence of compounds having energy states that are below the conventionally accepted ground state level. It is emphasized that Endnote 1 of the Appendix shows that Schrodinger's wave equation mandates that the value of "n" (or 1/p) must be a positive integer having the

values 1, 2, 3, and so on, and Endnote 5 shows that fractional values for "n" (or 1/p) are also impermissible in light of the Uncertainty Principle. The fourth full paragraph on page 19-14 of Bethe and Salpeter's Quantum Mechanics of One-and Two-Electron Atoms (Plenum Publishing Corp., New York, 1977) states that the "ground state" of hydrogen has n=1. It is clear from the foregoing that fractional values for "n" (or 1/p) cannot exist according to conventional scientific theories. Once the Patent and Trademark Office shows through scientific reasoning that an invention is inoperative, the burden then shifts to applicant to provide satisfactory evidence of operability of the invention. Newman v. Quigq, 877 F. 2d 1575, 11 USPQ 2d 1340 (Fed. Cir. 1989).

35 U.S.C. § 112 PARAGRAPH 1 REJECTION

Claims 1-28 are rejected under 35 U.S.C. § 112, first paragraph, as containing subject matter which was not described in the specification in such a way as to enable one skilled in the art to which it pertains, or with which it is most nearly connected, to make and/or use the invention. The specification does not enable one of ordinary skill in the art to make or use a "positive, negative or neutral increased binding energy atom" as recited in applicant's claims, in that it would require undue experimentation to do so. Factors to be considered in determining whether the disclosure would require undue experimentation

include (1) the quantity of experimentation necessary; (2) the amount of direction or guidance presented; (3) the presence or absence of working examples; (4) the nature of the invention; (5) the state of the prior art; (6) the relative skill of those in the art; (7) the predictability or unpredictability of the art; and (8) the breadth of the claims. In re Wands, 858 F. 2d 731, 737; 8 USPQ 2d 1400, 1404 (Fed. Cir. 1988). Each of these factors outlined in Wands will be addressed as to their relevance to the lack of enablement for applicant's claims.

Factor (1) THE QUANTITY OF EXPERIMENTATION NECESSARY

Pages 17-37 of applicant's specification disclose a gas cell reactor, a gas discharge cell reactor, and a plasma torch cell reactor for producing the claimed compounds. However, there are not sufficient details of the reaction conditions set forth on pages 17-30 which would allow one to produce and recover the claimed increased binding energy species.

Factor (2) THE AMOUNT OF DIRECTION OR GUIDANCE PRESENTED

The direction or guidance provided in the specification is found on pages 17-30, and is insufficient for the same reasons given hereinbefore with respect to Factor (1). In short, there are insufficient details of the reaction conditions provided to direct or guide one of ordinary skill in the art to produce the claimed compounds.

Factor (3) THE PRESENCE OR ABSENCE OF WORKING EXAMPLES.

The specification contains, on pages 17-30, examples of methods for forming and identifying the claimed increased binding energy species. It is unclear however whether applicant has actually formed and identified their increased binding energy species. The present examples are thus not considered to be working examples.

Factor (4) THE NATURE OF THE INVENTION

The scientific community has held the belief for decades that hydrogen cannot exist below the "ground state" (n = 1). same would be true for the elements lithium, beryllium and helium. (See the reasoning presented hereinbefore with respect to the rejection under 35 U.S.C. § 101 for inoperability and the Appendix.) Accordingly the nature of the invention is such that it would be startling if it were operative, thus requiring greater detail than that found on pages 17-30 of the specification for one of ordinary skill in the art to make and use the claimed invention without undue experimentation. Applicant himself points out that the Mills theory predicts the existence of a previously unknown form of matter: hydrogen atoms and molecules having electrons of lower energy than the conventional "ground" state, called "hydrinos" and "dihydrinos", respectively, where each energy level corresponds to a fractional quantum number. (See the paragraph bridging pages 13 and 14 of

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R. L. Mills, <u>The Grand Unified Theory of Classical Quantum</u>
<u>Mechanics</u> (BlackLight Power, Inc., New Jersey, 1999)).

Factor (5) THE STATE OF THE PRIOR ART

There appears to be <u>no</u> prior art showing hydrogen with a quantum number below 1, or even any prior art which would suggest that hydrogen with a quantum number below 1 could even exist in theory. See the Attached Appendix. Applicant himself points out that the Mills theory predicts the existence of a <u>previously unknown</u> form of matter: hydrogen atoms and molecules having electrons of lower energy than the conventional "ground" state, called "hydrinos" and "dihydrinos", respectively, where each energy level corresponds to a fractional quantum number. (See the paragraph bridging pages 13 and 14 of R. L. Mills, <u>The Grand Unified Theory of Classical Quantum Mechanics</u> (BlackLight Power, Inc., New Jersey, 1999)).

Factor (6) THE RELATIVE SKILL OF THOSE IN THE ART

Even the most highly skilled physicists were of the opinion that hydrogen (or any other element) cannot exist below the "ground state" (n = 1).

Factor (7) THE PREDICTABILITY OR UNPREDICTABILITY OF THE ART

It would be most unpredictable that the hydrogen atom (or any other element) could exist below the "ground state" (n = 1). (See the reasoning presented hereinbefore with respect to the

rejection under 35 U.S.C. § 101 for inoperability and the Appendix.)

Factor (8) THE BREADTH OF THE CLAIMS

The claims require the presence of at least one "increased binding energy species". It has been shown hereinbefore with respect to the rejection under 35 U.S.C. § 101 for inoperability that the hydrino atom cannot exist. Such increased binding energy species could therefore also not exist for one-electron atoms having an atomic mass of at least four, such as helium lithium or beryllium.

Considering all of the above factors, one skilled in the art could not make and/or use the claimed invention without undue experimentation.

35 U.S.C. § 112 PARAGRAPH 2 REJECTION

Claims 1-28 are rejected under 35 U.S.C. § 112, second paragraph, as being indefinite for failing to particularly point out and distinctly claim the subject matter which applicant regards as the invention. It is indefinite as to what would constitute an "increased binding energy species" (i.e., increased over what?). It is also indefinite as to what would constitute the "corresponding ordinary species".

Any inquiry concerning this communication or earlier communications from the examiner should be directed to Wayne A. Langel whose telephone number is (703) 308-0248. The examiner

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can normally be reached on Monday through Friday from 8 A.M. to 3:30 P.M.

If attempts to reach the examiner by telephone are unsuccessful, the examiner's supervisor, Steven Griffin, can be reached on (703) 308-1164. The fax phone number for this Group is (703) 305-7718.

Any inquiry of a general nature or relating to the status of this application or proceeding should be directed to the Group receptionist whose telephone number is (703) 308-2351.

WAL:cdc

January 15, 2002

Mayne A. Langel Wayne A. Langel Wayne A. Langel Primary Examiner GAU 1754

Appendix

Classical Quantum Mechanics (Blacklight Power Inc., New Jersey, 1999; hereafter, "GUT") which describes the existence of new energy states for the hydrogen atom that are below the conventionally accepted ground state energy. A hydrogen atom in any one of these new energy states is termed a "hydrino." According to equations (I.75a-c) on pages 19-20 of GUT, the general formula representing the energy levels for an electron with a principal quantum number, n, around the nucleus of the hydrogen atom is:

$$E_n = - (Rydberg constant)/n^2 = -13.6 electron volt/n^2$$

where n = 1, 2, 3, etc and n is also = 1/2, 1/3, 1/4, etc. While the former integer values of n give energies that are conventionally understood and experimentally verified, the latter fractional values of n lead to the energies of the electron in a hydrino atom which, according to Mills, represents a new "lower energy hydrogen atom."

A review of some of the main mathematical underpinnings in GUT shows that there is really no proper theoretical basis to assert the existence of the hydrino atom in view of the following discussion.

Nowhere has Mills satisfactorily established that fractional values of n arise as a natural consequence of a logical and internally consistent mathematical and scientific framework. While GUT bristles with a dense array of mathematical equations, the fractional values of n are not shown to be the unequivocal end result of Mills' theory. It appears that there is an internal break in logic in the mathematical analysis, with Mills ultimately relying on conclusionary statements, such as, a nonradiative boundary condition and the relationship between the electron and a photon gives transitions in which the electron goes to a "lower" energy nonradiative state with a smaller radius or, alternatively, that an electron can undergo a collision with an "energy hole" which allows the electron to undergo a transition to a lower energy nonradiative state with a smaller radius (pages 16-17 of GUT). In these transitions,

accompanied by the release of energy. See pages 16, 17 and 144-146 of GUT.

By way of background, it is noted that there are at least two conventionally recognized approaches to the problem of obtaining the energy levels of the electron in the hydrogen atom. These are:

- (a) Via a Differential Equation approach formulated as a two-point boundary value problem where boundary conditions at the nucleus and at infinity are imposed on the radial wavefunction of the electron which satisfies a second-order linear differential equation known as Schrödinger's wave equation. It is to be understood that while the complete wavefunction in spherical polar coordinates is the product of a radial wavefunction and angular wavefunctions, the complete wavefunction for the ground (or lowest energy) state of the hydrogen atom is independent of angular coordinates in view of the spherical symmetry of that state, and is studied only on the basis of the radial wavefunction. Thus, see attached sections 18d-18e and 21b at pages 121-124 and 139 from Pauling and Wilson's Introduction to Quantum Mechanics (Dover Publications, Inc., New York, 1985) and Endnote 1.
- (b) Via an Integral Equation approach wherein the boundary conditions on the radial wavefunction of the electron are "built into" the integral equation itself rather than being imposed on it as in the differential equation formulation. In this approach, upon taking the Fourier transform of the wavefunction, subject to the boundary condition that it satisfies Schrödinger's equation, an integral equation is obtained. Thus, see attached pages 899-900 from Morse and Feshbach's Methods of Theoretical Physics, Part I (McGraw-Hill Book Company, New York, 1953) and Endnote 2.

It is crucial to note that either approach is but a mathematical tool and that, while the integral equation approach may be mathematically more compact and, perhaps, be more convenient for solving certain problems compared to the differential equation approach, the

final results given by either approach must not be mutually contradictory if a scientific theory based on these approaches is to be logical and internally consistent.

From a consideration of Mills' mathematical derivations on pages 4-5 (equations (I.5) to (I.11)), on pages 32-38 (equations (1.3) to (1.45)) and on pages 136-141 (equations (5.1) to (5.21)) of GUT, it appears that Mills' formulation may be an integral equation type of approach. Specifically, the boundary condition "built into" the integral equation is an expression for the current density, and, thus, the charge density of a point charge which satisfies Maxwell's equation for the electric field as given by Haus in a paper, in the American Journal of Physics, vol. 54, no. 12, pages 1126-1129 (1986), relating to the absence of radiation from a point charge moving at constant velocity. See page 3 of GUT. While, Haus' paper is not the focus of discussion here, it is apparent that the use of a Dirac delta function, $\delta(r-r_n)$, to represent the electron charge density on page 4 of GUT may be an unphysical assumption in that, whereas the electron charge density is an "observable" that is ultimately measurable, the delta function, which purports to represent it, is not, in and of itself, a function in the usual mathematical sense of the term and is physically meaningful only under an integral sign.

More specifically, it appears that Mills' integral equation approach utilizes the technique of the "Green's function." In the theory of integral equations, the Green's function is a function that satisfies a differential equation involving a Dirac delta function type of point source. A connection between the Green's function and the wavefunction is established by requiring the former to satisfy boundary conditions corresponding to those satisfied by the latter. Interpreting Mills' equations as best as one can, it is possible, though by no means certain, that Mills achieves such a connection by requiring the Green's function to satisfy boundary conditions imposed on the charge density function in Mills' equation (1.1) on page 31 of GUT. The final step in the integral equation approach is to generate an integral

equation involving an integral taken over the Green's function. The solution of that equation would yield the wavefunction of the electron and, from that, leads to the energy levels of the electron in the hydrogen atom. See attached pages 808, 902 and 903 from Morse and Feshbach op. at. and Endnote 3. It is observed that the legitimate use of a Green's function which satisfies an equation involving a Dirac delta function type of "point source" and appears, ultimately under an integral sign as the kernel of an integral equation, does not justify Mills' representation of the electron charge density, which is a "smeared out" charge distribution, as a Dirac delta function as discussed previously. Mills' lack of consistency in using properly subscripted variables as well as the absence of a logical flow in the mathematical derivations, prevents one from properly assessing the kind of approach taken in GUT.

In any event, at least some problematical issues are seen in the Mills' treatment, $ni\chi$, (i) it is not explained as to why it is physically meaningful to utilize Haus' boundary condition for a classical point charge moving in free space in order to obtain the energy levels of the electron in a quantized system such as the hydrogen atom where the electron moves in a confined space due to its attractive coulombic interaction with the positively charged nucleus, and, (ii) there is no explanation for the catastrophic collapse of the electron into the nucleus as $n \to \infty$ in the fractional quantum number series, 1/n, i.e. the hydrino atom implodes and ceases to exist. See pages 144-146 of GUT. The end result of Mills' integral equation approach, if such it is, fails to bear out his assertion that n must unequivocally have fractional values. In essence, it appears that the condition that n have fractional values (see equations (1.75c) and (2.2) on pages 20 and 81 of GUT) is but an *ad hoc* statement that does not logically flow from Mills' derivation of the equation for the energy levels of the electron in the hydrogen atom and it may even represent a type of forced parameterization scheme

deliberately structured to produce a desired outcome contrary to the logical flow of its mathematics or, even, common sense.

Hence, it appears that Mills' theory remains essentially unproven as discussed above and does not constitute a proper basis to demonstrate the existence, at least on theoretical grounds alone, of the so-called hydrino atom.

Furthermore, Mills' theory does not show that the conventional quantum mechanical treatment of the hydrogen atom is theoretically or experimentally flawed. Any attempt to establish a new result for the hydrogen atom that is presently unknown to quantum mechanics must cross a rather steep threshold of scientific credibility. See the attached page 2 from Bethe and Salpeter's *Quantum Mechanics of One- and Two-Electron Atoms* (Plenum Publishing Corporation, New York, 1977 and Endnote 4.

Among the many problems solved by quantum mechanics, the hydrogen atom, along with the linear harmonic oscillator and the particle-in-a-box, is one of the few scientific problems that has received extensive theoretical and experimental treatment over many years since the first decade of the twentieth century. For a complete treatment of the hydrogen atom problem see the attachment from pages 19-1 to 19-18 of Feynman's *Lectures in Physics*, vol. III, Quantum Mechanics (Addison-Wesley Publishing Co., Reading, Mass., 1965). The results obtained from at least one type of standard procedure for solving the radial Schrödinger equation using a power series expansion for the wavefunction of the electron inescapably lead to the conclusion that only positive integer values for n are permissible (as explained previously in Endnote 1). See attached pages 1-9 and 2-6 from Feynman op. cit. and Endnote5. In other words, conventional theory and experiment forbid hydrino atoms.

Endnote 1

Schrödinger's wave equation for the radial wavefunction, S(Q), is:

$$(1/\varrho^2)(d/d\varrho)(\varrho^2dS/d\varrho) + \{-1/4 - l(l+1)/\varrho^2 + \lambda/\varrho\}S = 0$$

where ϱ is proportional to the radial coordinate in the spherical polar coordinate system with $0 \le \varrho \le \infty$, I is the orbital angular momentum quantum number and λ is proportional to negative (i.e. bound) energy values. The boundary conditions are that far from the nucleus of the hydrogen atom $(\varrho \to \infty)$ the radial wavefunction becomes negligible i.e. S $\to 0$, and, at the nucleus of the atom ($\varrho = 0$), noting that S is expressible as $e^{-\varrho/2}\varrho^t L(\varrho)$ where $L = \sum_{\alpha} a_{\alpha}\varrho^{\alpha}$ is an infinite power series in Q, substitution of the expression for S into the radial wavefunction equation results in the choice of s = +l (which is a positive integer) as the only choice that will permit to be S be an acceptable wavefunction, which in turn yields the boundary condition that S has a finite value at the nucleus. Note that despite the finite value of the radial wavefunction at the nucleus, the probability of finding the electron at the nucleus, $\varrho = 0$, of the hydrogen atom in its normal ground state is proportional to $4\pi\varrho^2 S^2$ which, of course, is zero. Upon substituting the cited expression for S into the radial wavefunction equation, recursion relations between a_{ν} for various values of ν are obtained. The recursion relations contain the principal quantum number n appearing as a multiplicative coefficient of a. Since S must have a proper asymptotic behavior as $\varrho \to \infty$, this requires that the infinite power series be terminated after a finite number of terms which in turn, after some algebra, leads to the result that n must be a positive integer having the values 1, 2, 3, etc.. See equations (18.29) to (18.39) and Figure 21-1 at pages 121-124 and 140 in Pauling and Wilson.

Endnote 2

Substitution of the Fourier transform of the wavefunction, $\psi(\mathbf{r})$, viz.

$$\psi(\mathbf{r}) = (1/\hbar)^{3/2} \int_{-\infty}^{\infty} \varphi(\mathbf{p}) e^{(2\pi i/\hbar)\mathbf{p}.\mathbf{r}} d\mathbf{p},$$

where b is Planck's constant and \mathbf{p} and \mathbf{r} are momentum and spatial coordinate vectors, respectively, into the Schrödinger equation in the differential form

$$\nabla^2 \psi + (2m/b^2) \{ \mathbf{E} - \mathbf{V}[\mathbf{r}, (b/2\pi i)\nabla] \} \psi = 0,$$

where ∇^2 , E and V are the Laplacian operator, total and potential energies, respectively, followed by multiplication through by $(1/b)^{3/2} e^{(-2\pi i/b)q \cdot \mathbf{r}}$ and an integration over \mathbf{r} yields the desired integral equation

$$(q^2/2m)\varphi(\mathbf{q}) + \int_{-\infty}^{\infty} \varphi(\mathbf{p})V(\mathbf{p}-\mathbf{q}, \mathbf{p})d\mathbf{p} = E\varphi(\mathbf{q})$$

where

$$V(\mathbf{p}-\mathbf{q},\mathbf{p}) = (1/h)^{3/2} \int_{-\infty}^{\infty} e^{(2\pi i/h)(\mathbf{p}-\mathbf{q})\cdot\mathbf{r}} V(\mathbf{r},\mathbf{p}) d\mathbf{r}$$

with q being a momentum vector.

See equation (8.1.4) at page 900 in Morse and Feshbach.

Endnote 3

To illustrate a method of obtaining a solution for the wavefunction, ψ , by the technique of Green's functions consider the Schrödinger equation for ψ written as:

$$[\nabla^2 + k^2]\psi = U\psi$$

where $k^2 = (8\pi^2 \text{m/}b^2)\text{E}$ and $U = (8\pi^2 \text{m/}b^2)\text{V}$ with E and U being the total and potential energies, respectively. A Green's function, $G_k(\mathbf{r}|\mathbf{r}_0)$, is introduced which satisfies

$$[\nabla^2 + k^2]G_k(\mathbf{r}|\mathbf{r}_0) = -4\pi\delta(\mathbf{r}-\mathbf{r}_0),$$

where $\delta(\mathbf{r}-\mathbf{r}_0)$ is a Dirac delta function representing a "point source" at \mathbf{r}_0 . The Green's function can be thought of as representing an effect at \mathbf{r} caused by a point source at \mathbf{r}_0 . The

boundary conditions on $G_k(\mathbf{r} | \mathbf{r}_0)$ are chosen to be the same as those corresponding to the boundary conditions on the wavefunction ψ . Then, by the theory of integral equations, a solution to the Schrödinger equation is:

$$\psi({\bm r}) = -(1/4\pi) \int \; G_{{\bm k}}({\bm r} \,|\, {\bm r}_0) U({\bm r}_0) \; \psi({\bm r}_0) {\rm d}{\bm r}_0. \label{eq:psi_psi_supplied}$$

See pages 808, 902 and 903 in Morse and Feshbach.

Endnote 4

Regarding the study of the hydrogen atom, note the following quotation from page 2 of Bethe and Salpeter's classic text entitled *Quantum Mechanics of One- and Two-Electron Atoms* (Plenum Publishing Corporation, New York, 1977):

"One of the simplest, and most completely treated, fields of application of quantum mechanics is the theory of atoms with one or two electrons. For hydrogen and the analogous ions He⁺, Li⁺⁺, etc., the calculations can be performed exactly, both in Schrödinger's nonrelativistic wave mechanics and in Dirac's relativistic theory of the electron. More specifically alculations are exact for a single electron in a fixed Coulomb potential. Hydr gen-like atom hus furnish an excellent way of testing the validity of quantum chanics. For such atom the correction terms due to the motion and structure of atomic nuclei and due to quantum electrodynamic effects are small and can be calculated with high accuracy. Since the energy levels of a rogen and similar atoms can be investigated experimentally to an astounding degree or arracy, some accurate tests of the validity of quantum electrodynamics are also possible."

Endnote 5

It is noteworthy that this position is also supported by a different line of argument that is independent of the solution to Schrödinger's equation. Thus, fractional values for the principal quantum number n would bring the electron much closer to the nucleus of the hydrogen atom than is permitted by Heisenberg's Uncertainty Principle. Feynman has presented a mathematically simple argument, in his "Lectures in Physics," vol. III, page 2-6, to show that the size of the hydrogen atom i.e. when n is 1 (rather than, say, 1/2) is perfectly consistent with the Uncertainty Principle. This argument goes as follows: from the Uncertainty Principle, if the electron is at a distance a from the hydrogen nucleus, then the product of its momentum and a must be of the order of Planck's constant. Now the total energy of the electron is the sum of its kinetic and potential energies. Noting that the kinetic energy can be expressed in terms of the square of the momentum, upon invoking the value of the momentum from the Uncertainty Principle and minimizing the total energy in order to obtain the lowest energy level of the electron, one immediately obtains the standard result for the lowest energy level of the electron in the hydrogen atom which is consistent with nbeing 1 and no lower than 1. Since, according to Feynman, "no one has ever found (or even thought of) a way around the Uncertainty Principle ... so we must assume it describes a basic characteristic of nature," (page 1-9 in Feynman) it appears that Mills' fractional value for n is impermissible in light of the inviolability of the Uncertainty Principle.